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### Appendix 1: Additional sample tasks

### Task 8: Ability to critically evaluate a presented solution to a problem/question

Examine critically the following question and a solution presented by a student. Indicate clearly your comments on the presented solution with justification. Also present your alternative solution to the question.

Question: Find the derivative of  $x \sin x$  with respect to x

Solution:  $\frac{d}{dx}(x \sin x) = \frac{d}{dx}(x) \frac{d}{dx}(\sin x) = 1 \cos x = \cos x$ 

## Task 9: Ability to use with reasonable skill available tools for mathematical exploration

Use the graph which is a representation of the function f'(x) to determine features related to the relative extrema and concavity for the original function defined by y = f(x)



### Task 10: Ability to identify linkages between groups of concepts and interpret these linkages in the context of a model

For functions defined by equations of the form y = f(x), what could be concluded from the following?

- 1. f(0)
- 2. f(x) = 0
- 3. the rational function defined by y = f(x) has domain  $(-\infty, -1) \cup (-1, 2) \cup (2, \infty)$
- $4. \quad \lim_{x \to 2^+} f(x) = \infty$
- 5.  $\lim_{x \to \infty} f(x) = 2$
- 6. f'(x)
- 7. f'(x) < 0 on the interval [a, b]
- 8. f''(x) < 0 on the interval [c, d]
- 9. f''(m) < 0 for some value *m* in the domain of the function *f*

# Task 11: Ability to identify linkages between groups of concepts and interpret these linkages in the context of a model

Use appropriate geometric figures to interpret and evaluate the following definite integral

$$\int_{0}^{3} \left(4 - \sqrt{9 - x^2}\right) dx$$