# CHANNEL AND DELAY ESTIMATION FOR BASE-STATION-BASED COOPERATIVE COMMUNICATIONS IN FREQUENCY FLAT-FADING CHANNELS

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## ABSTRACT

Base-station-based cooperative communication is an asynchronous cooperative communication system. The challenge therein is to estimate the relative delay between the transmitters in the system. A channel and delay estimation algorithm based on the distributed Alamouti scheme has been previously discussed for the asynchronous cooperative system. The algorithm only makes accommodation for positive delay, that is, when data from Transmitter one always arrives at the receiver before data from Transmitter two. In reality, the data from Transmitter one does not always arrive at the receiver before data from Transmitter two in the asynchronous cooperative system, because of the constantly changing mobile environment in the system. This paper extends the algorithm to accommodate both positive and negative delays, which is when the data from Transmitter one arrives at the receiver *before* or *after* data from Transmitter two, in a Rayleigh block flat-fading channel. Simulation results show that the Cramér–Rao lower bound for channel and delay estimation is achieved for different delay values. The symbol error rate performance is also achievable compared to the channel and the delay is known at the receiver.

# I. INTRODUCTION

Cooperative diversity is a relatively new transmission scheme that combines the ideas of relays and multiple antennas, while avoiding the size limitations of a single mobile node. It provides spatial diversity by allowing multiple nodes, each with a single antenna (it is possible to increase the number of antennas), to work together to form a virtual multiple-input–multiple-output (MIMO) system. Sendonaris et al.<sup>12</sup> have shown that even with a noisy inter-user channel, cooperative communication still leads to improved performance, and is generally a more robust system. One real MIMO system is the space-time block code (STBC) system, which achieves both space and time diversity. If both STBC and cooperative diversity are incorporated together, a distributed STBC system is formed.<sup>34</sup>

In this paper, we focus on cooperative communication using the Alamouti scheme,<sup>5</sup> which is a specialcase, full-rate orthogonal STBC with two transmit antennas and one receive antenna. A typical example of the system is a base-station-based cooperative communication in macrocell downlink networks, which is proposed by Skjevling et al.<sup>6</sup> In the base-station-based cooperation system, all base stations are connected via a very fast-wired local area network and are setup to transmit data to one mobile user. Skjevling et al.<sup>6</sup> discussed a precoded distributed STBC synchronous cooperative diversity system. But in reality this scenario is unlikely. The challenge therein is to estimate the relative delay between the transmitters in the system. This problem has been addressed, which resulted in a channel and delay estimation algorithm that achieved the lower Cramér–Rao bound (CRB).<sup>7</sup> Tourki and Deneire provided a simple maximum likelihood channel and delay estimation algorithm, but this system was only derived for positive delays, that is, when Transmitter one's data always arrives at the receiver *before* Transmitter two's data.<sup>7</sup>

The main motivation behind this paper is to extend the scheme in Tourki and Deneire<sup>7</sup> to accommodate negative delays (i.e. when Transmitter two's data arrives at the receiver *before* Transmitter one's data). This extension is significant, for example, in the case of a macrocell, as considered in this paper. Specifically, the macrocell considered here consists of two base stations transmitting the same data to one node. Since the node is mobile, it could be closer to either base station at any given time, and it cannot be arbitrarily assumed that the first signal it receives is from base station one, as the Alamouti's scheme<sup>5</sup> strictly dictates the role of each of the two transmitters in the transmission scheme. By extending the delay estimation search to negative delays, the receiver can determine which transmitter's data arrived first, and hence properly decode the received signals.

This paper is structured as follows: in Section II, the system model of Tourki and Deneire<sup>7</sup> is extended to accommodate negative delays, in Section III the channel and delay estimation algorithm for both positive and negative delays is derived, in Section IV the detection scheme for a single receiver is shown, in Section V the symbol error probability is discussed, in Section VI the simulation results are presented and, finally, in Section VII the conclusions are drawn.

# **II. SYSTEM MODEL**

The system model consists of two base stations (BS1 and BS2) transmitting data to one mobile node, each with a single transceiver.<sup>7</sup> The channel gains from BS1 and BS2 to the mobile node are  $h_1$  and  $h_2$ , respectively, where  $h_1$  and  $h_2$  are assumed to be the complex scalar channel parameters. It is assumed that both base stations have knowledge of both pilot sequences  $\mathbf{d}_1$  and  $\mathbf{d}_2$ . In reality, this can be achieved via either a wired, high-speed connection such as Ethernet, or a wireless transmission of the data between two base stations preceding the transmission scheme presented here.

The data sequences to be transmitted are replicated in space and time according to the time-reversed block form of the Alamouti's scheme,<sup>5</sup> allowing the mobile node to combine and decode the two



FIGURE 1 Data transmission model



FIGURE 2 Block transmission

received signals, using a simple linear technique while enjoying the benefits of spatial diversity.

The data transmission model is shown in Figure 1. To begin with, the data set to be transmitted is parsed into two blocks  $\overline{of N}$ symbols each,  $\mathbf{d}_n$  and  $\mathbf{d}_{n+1}$ , where *n* is the block number. Training symbols  $\mathbf{d}_1$  and  $\mathbf{d}_2$ , each of length L, are then added at the end of  $\mathbf{d}_{n}$  and  $\mathbf{d}_{n+1}$ , respectively, to form two  $(N+L) \times 1$  vectors. To insert a cyclic prefix of training symbols between any two successive blocks, these vectors are pre-multiplied by a precoding matrix  $\mathbf{F}_{\mathbf{p}}$ . Multiplying the vectors by  $\mathbf{F}_{\mathbf{p}}$  results in two  $(N + 2L) \times 1$ blocks,  $\mathbf{s}_n$  and  $\mathbf{s}_{n+1}$ .

The blocks are then transmitted according to the time-reversed block form of the Alamouti's scheme shown in Figure 2. In Figure 2, (.)\* indicates the complex conjugate operator.

The precoding matrix F<sub>n</sub> and time-reversal matrix T<sup>7</sup> are given by

$$\mathbf{F}_{p} = \begin{bmatrix} \mathbf{O}_{LXN} & \mathbf{I}_{L} \\ \mathbf{I}_{N+L} \end{bmatrix}$$
[Eqn 1]

T 
$$(k, N+2L+1-k) = 1$$
,  $k = 1, \dots, N+2L$  [Eqn 2]

where  $\mathbf{O}_{L \times N}$  is a ( $L \times N$ ) matrix of zeros,  $\mathbf{I}_{L}$  and  $\mathbf{I}_{N+L}$  are identity matrices of dimensions  $(L \times L)$  and  $(N + L) \times (N + L)$ , respectively.

By defining  $\tau = \tau_2 - \tau_1$  as the difference between the arrival time of the two signals, where  $\tau_1$  and  $\tau_2$  are the arrival times of the first (BS1) and second (BS2) signal respectively, the received signal r can then be defined as7

$$\mathbf{r} = \mathbf{A}(\tau)\mathbf{X}\mathbf{h} + \mathbf{b}$$
 [Eqn 3]

where  

$$\mathbf{X} = \begin{bmatrix} x & \mathbf{0}_{2N+4L} \\ \mathbf{S}_{n} & \mathbf{0}_{N+2L} \\ -\mathbf{T}(\mathbf{s}_{n+1})^{*} & \mathbf{0}_{N+2L} \\ \mathbf{0}_{2N+4L} & x \\ \mathbf{0}_{N+2L} & \mathbf{S}_{n+1} \\ \mathbf{0}_{N+2L} & \mathbf{T}(\mathbf{s}_{n})^{*} \end{bmatrix}$$
[Eqn 4]

and  

$$\mathbf{h} = \begin{bmatrix} h_1 \\ h_2 \end{bmatrix}$$
[Eqn 5]

In [Eqn 3] to [Eqn 5], **r** is a symbol vector of length (2N + 4L);  $\tau \in [-(L-1), L-1]$  is the relative delay between the two received signals;  $h_i$ , i = 1, 2, are the zero mean complex scalar channel parameters. They are also assumed to be Rayleigh block flatfading, that is, the amplitude of the fading envelope follows a Rayleigh distribution which stays constant for the duration of each frame, but varies independently from frame to frame. In [Eqn 3], b is assumed to be zero mean complex additive white Gaussian noise (AWGN), with each entry having a variance of  $N_0/2$  per dimension, while **X** is the data matrix where *x* denotes symbols from the previous frame which are treated as 'don'tcares'. The matrix  $A(\tau)$ , denotes the delay matrix.

For positive delay  $A(\tau)$  is given by

$$\mathbf{A}(\tau) = (\mathbf{O}_{2N+4L} \mathbf{I}_{2N+4L} \mathbf{\Gamma} \mathbf{\Psi}) \text{ for } \tau \ge 0$$
 [Eqn 6]

where

$$\Gamma = \begin{bmatrix} \mathbf{O}_{|\tau| \times (2N+4L - |\tau|)} & \mathbf{I}_{\tau} \\ \mathbf{O}_{(2N+4L - |\tau|) \times (2N+4L - |\tau|)} & \mathbf{O}_{(2N+4L - |\tau|) \times |\tau|} \end{bmatrix}$$
and
$$[Eqn 7]$$

$$\Psi = \begin{bmatrix} \mathbf{O}_{|\tau| \times (2N+4L_{-}|\tau|)} & \mathbf{O}_{\tau} \\ \mathbf{I}_{2N+4L_{-}|\tau|} & \mathbf{O}_{(2N+4L_{-}|\tau|) \times |\tau|} \end{bmatrix}$$
 [Eqn 8]

where  $|\cdot|$  is the absolute value operator.

It is worthwhile to note that for the synchronous case,  $\Gamma = O_{2N+4I}$ and  $\Psi = \mathbf{I}_{2N+4L}$ .

To extend the received signal model to accommodate negative delays, one needs only to modify [Eqn 6]. To understand this extension, one first needs to understand how [Eqn 6] accounts for the asynchronicity of the system. Figure 3 shows the illustration of  $A(\tau)$  for  $\tau \ge 0$ .

In Figure 3, the dashed-dotted lines represent ones and blank spaces represent zeros in the corresponding matrices.

When  $A(\tau)$  is multiplied by the data matrix **X**, for  $\tau \ge 0$  it can be seen that the received signal from BS1 will just be  $s_1[n]$ , but from BS2, the delayed  $\tau$  symbols from the previous frame [ $s_2(n-1)$ ] are received first and the last  $\tau$  symbols of  $s_2[n]$  will be received in the next frame.

For negative delays, only the symbols from BS1 will be delayed, and hence the resulting equation for  $A(\tau)$  is

$$\mathbf{A}(\tau) = (\Gamma \ \Psi \ \mathbf{O}_{2N+4L} \ \mathbf{I}_{2N+4L}) \text{ for } \tau < 0$$
 [Eqn 9]



 $\begin{array}{l} \mbox{FIGURE 3} \\ \mbox{Illustration of } A(\tau) \mbox{ for } \tau \geq 0 \end{array}$ 

Figure 4 shows the illustration of  $A(\tau)$  for  $\tau < 0$ . Once again, the dashed-dotted lines represent ones, and blank spaces represent zeros in the corresponding matrices.

# III. CHANNEL AND DELAY ESTIMATION ALGORITHM

A maximum likelihood (ML) estimator used by Tourki and Deneire<sup>7</sup> and Sirbu<sup>8</sup> is also used for the channel and delay estimation in this section. Firstly we summarise the estimation algorithm of Tourki and Deneire<sup>7</sup> for  $\tau \ge 0$ , and then use the same approach to derive the estimation algorithm for  $\tau < 0$ . Let **ts**<sub>1</sub> and **ts**, be defined as

$$\mathbf{ts}_1 = \mathbf{T}_2 \mathbf{d}_1$$
 [Eqn 10]

$$\mathbf{ts}_2 = \mathbf{T}_s \mathbf{d}_2$$
 [Eqn 11]

where  $\mathbf{T}_s$  is a time-reversal matrix of size *L* (i.e.  $\mathbf{T}_s$  is basically a small version of the matrix **T**).

The section of the received signal where the pilot symbols from each transmitter overlap are defined as  $S(\tau) = [ss_1(\tau) ss_2(\tau)]$ . For convenience, 'L<sub>1</sub>:L<sub>2</sub>' is defined as a sequence from index L<sub>1</sub> to L<sub>2</sub>.

Figure 5 shows  $S(\tau)$  for  $\tau \ge 0$ , where  $ss_1$  and  $ss_2$  are defined as

$$\mathbf{ss}_{1} = \begin{bmatrix} \mathbf{d}_{1}(\tau+1:L) \\ -\mathbf{ts}_{2}^{*} \end{bmatrix}$$
 [Eqn 12]  
and

$$\mathbf{ss}_{2} = \begin{bmatrix} \mathbf{d}_{2} \\ [\mathbf{ts}_{1}(1:L-\tau)]^{*} \end{bmatrix}$$
 [Eqn 13]

![](_page_2_Figure_14.jpeg)

 $\label{eq:FIGURE 5} \begin{array}{l} \mbox{FIGURE 5} \\ \mbox{Illustration of } S(\tau) \mbox{ for } \tau \geq 0 \end{array}$ 

![](_page_2_Figure_16.jpeg)

Figure 6 shows  $S(\tau)$  for  $\tau < 0$ . From Figure 6, it is observed that the symbols from BS1 are shifted.

The modified equations for  $ss_1$  and  $ss_2$  for  $\tau < 0$  are given by

$$\mathbf{ss}_{1} = \begin{bmatrix} \mathbf{d}_{1} \\ -[\mathbf{ts}_{2}(\mathbf{ts}_{2}(1:L-|\tau|)]^{*} \end{bmatrix}$$
 [Eqn 14]  
$$\mathbf{ss}_{2} = \begin{bmatrix} \mathbf{d}_{2}(|\tau|+1:L) \\ \mathbf{ts}_{1}^{*} \end{bmatrix}$$
 [Eqn 15]

From Figures 5 and 6, one can define  $\mathbf{z}(\tau)$  as  $\mathbf{z}(\tau) = \mathbf{S}(\tau)\mathbf{h} = \mathbf{r}(N + L + |\tau| + 1: N + 3L)$ . It then follows that<sup>7</sup>

$$\tilde{\mathbf{h}}(\tau) = [\mathbf{s}(\tau))]^{\#} \mathbf{z}(\tau)$$
[Eqn 16]

where [.]<sup>#</sup> represents the pseudo-inverse operator and  $\tilde{h}$  is the linear least squares estimate of h for a given value of  $\tau$ .

Since delay search space has been extended to accommodate negative delay values, the ML estimator used by Tourki and Deneire<sup>7</sup> and Sirbu<sup>8</sup> has to be modified to

$\hat{\boldsymbol{\tau}} = \arg\min_{ \boldsymbol{\tau}  < L}  \mathbf{z}(\boldsymbol{\tau}) \cdot \mathbf{S}(\boldsymbol{\tau}) \hat{\mathbf{h}}(\hat{\boldsymbol{\tau}}) ^2$	[Eqn 17]
and	

$$\hat{\mathbf{h}} = [\mathbf{S}(\hat{\tau})]^{\#} \mathbf{z}(\hat{\tau})$$
[Eqn 18]

where  $\hat{\mathbf{h}}$  is the final estimate of  $\mathbf{h}$  based on the delay estimate  $\hat{\boldsymbol{\tau}}$ .

The minimum square error (MSE) of the channel estimation is

![](_page_2_Figure_28.jpeg)

FIGURE 6 Illustration of  $S(\tau)$  for  $\tau < 0$ 

![](_page_3_Picture_0.jpeg)

given by

$$\mathbf{MSE} = \mathbf{E}[(\mathbf{h} \cdot \hat{\mathbf{h}})(\mathbf{h} \cdot \hat{\mathbf{h}})^{\mathrm{H}}]$$
 [Eqn 19]

where  $\mathbf{E}[.]$  is the expectation operator and H represents the conjugate and transpose operation.

# **IV. DETECTION SCHEME**

The data symbols are extracted and decoded as follows:

While ignoring the noise terms, define  $\mathbf{r}_{a}$  and  $\mathbf{r}_{b}$  as<sup>7</sup>

$$\mathbf{r}_{a} = \hat{h}_{1} \begin{bmatrix} \mathbf{d}_{n} \\ \mathbf{d}_{1}(1:\tau, 1) \end{bmatrix} + \hat{h}_{2} \begin{bmatrix} \mathbf{d}_{2}(\tau+1:L, 1) \\ \mathbf{d}_{n+1} \end{bmatrix} = \mathbf{r} \quad (L+1:N+L+|\hat{\tau}|, 1)$$
[Eqn 20]

$$\mathbf{r}_{b} = \hat{h}_{1} \begin{bmatrix} -\mathbf{T}_{N} \mathbf{d}_{n+1}^{*} \\ -\mathbf{t}\mathbf{s}_{2}^{*} (1;\tau,1) \end{bmatrix} + \hat{h}_{2} \begin{bmatrix} \mathbf{t}\mathbf{s}_{1}^{*}(\tau+1;L,1) \\ \mathbf{T}_{N} \mathbf{d}_{n}^{*} \end{bmatrix} = \mathbf{r} (N+3L+1:2N+3L+|\hat{\tau}|,1)$$
[Eqn 21]

where  $\mathbf{T}_{N}$  is a time-reversal matrix of size *N*.

For a clearer understanding,  $\mathbf{r}_{\rm a}$  and  $\mathbf{r}_{\rm b}$  are illustrated in Figures 7 and 8.

A block form of the decoding scheme has been derived here, and uses the same orthogonal system properties as the scheme in Tourki and Deneire<sup>7</sup>. As will be shown, the following block form also allows for a simple modification to accommodate negative delays.

Define  $\mathbf{r}_{w}$ ,  $\mathbf{r}_{v}$  and  $\mathbf{r}_{n}$  as

$$\mathbf{r}_{w} = \hat{h}_{i}^{*} \mathbf{r}_{a} = |\hat{h}_{i}|^{2} \begin{bmatrix} \mathbf{d}_{n} \\ \mathbf{d}_{1}(1:\tau, 1) \end{bmatrix} + \hat{h}_{i}^{*} \hat{h}_{2} \begin{bmatrix} \mathbf{d}_{2}(\tau+1:L, 1) \\ \mathbf{d}_{n+1} \end{bmatrix}$$
[Eqn 22]

$$\mathbf{r}_{x} = \hat{h}_{2}(\mathbf{T}_{r}\mathbf{r}_{b}^{*}) = -\hat{h}_{2}\hat{h}_{1}^{*} \begin{bmatrix} \mathbf{d}_{2}(\tau+1:L,1) \\ \mathbf{d}_{n+1} \end{bmatrix} + |\hat{h}_{2}|^{2} \begin{bmatrix} \mathbf{d}_{n} \\ \mathbf{d}_{1}(1:\tau,1) \end{bmatrix}$$
[Eqn 23]

$$\mathbf{r}_{n} = \mathbf{r}_{w} + \mathbf{r}_{x} = (|\hat{h}_{1}|^{2} + |\hat{h}_{2}|^{2}) \begin{bmatrix} \mathbf{d}_{n} \\ \mathbf{d}_{1}(1:\tau, 1) \end{bmatrix}$$
 [Eqn 24]

where T<sub>i</sub> is a square time-reversal matrix of size  $N + \tau$ , and r<sub>a</sub> and r<sub>b</sub> are defined in [Eqn 20] and [Eqn 21], respectively.

![](_page_3_Figure_18.jpeg)

FIGURE 7 Illustration of  $r_{_{a}}$  and  $r_{_{b}}$  for  $\tau \geq 0$ 

The estimate of  $\tilde{d}_n$  for  $\tau \ge 0$  is given by

$$\tilde{\mathbf{d}}_{n} = (|\hat{h}_{1}|^{2} + |\hat{h}_{2}|^{2}) \mathbf{r}_{n} (1:N,1)$$
 [Eqn 25]

Xu & Padayachee

Define  $\mathbf{r}_{y}$ ,  $\mathbf{r}_{z}$  and  $\mathbf{r}_{n+1}$  as

~

$$\mathbf{r}_{y} = \hat{h}_{2}\mathbf{r}_{a} = \hat{h}_{2}\hat{h}_{1} \begin{bmatrix} \mathbf{d}_{n} \\ \mathbf{d}_{1}(1:\tau,1) \end{bmatrix} + |\hat{h}_{2}|^{2} \begin{bmatrix} \mathbf{d}_{2}(\tau+1:L,1) \\ \mathbf{d}_{n+1} \end{bmatrix}$$
[Eqn 26]

$$\mathbf{r}_{z} = \hat{h}_{1}(\mathbf{T}_{r}\mathbf{r}_{b}^{*}) = -|\hat{h}_{1}|^{2} \begin{bmatrix} \mathbf{d}_{2}(\tau+1:L,1) \\ \mathbf{d}_{n+1} \end{bmatrix} + \hat{h}_{1}\hat{h}_{2}^{*} \begin{bmatrix} \mathbf{d}_{n} \\ \mathbf{d}_{1}(1:\tau,1) \end{bmatrix}$$
[Eqn 27]

$$\mathbf{r}_{n+1} = \mathbf{r}_{y} - \mathbf{r}_{z} = (|\hat{h}_{1}|^{2} + |\hat{h}_{2}|^{2}) \quad \begin{bmatrix} \mathbf{d}_{z}(\tau+1;L,1) \\ \mathbf{d}_{n+1} \end{bmatrix}$$
[Eqn 28]

Then the estimate of  $\tilde{d}_{n+1}$  for  $\tau \ge 0$  is given by

$$\widetilde{\mathbf{d}}_{n+1} = (|\hat{h}_1|^2 + |\hat{h}_2|^2) \mathbf{r}_{n+1} (\hat{\tau} + 1: \hat{\tau} + N, 1)$$
[Eqn 29]

Using a similar approach one can obtain the estimate of  $d_n$  and  $d_{n+1}$  for  $\tau < 0$  by

$$\widetilde{\mathbf{d}}_{n} = (|\hat{h}_{1}|^{2} + |\hat{h}_{2}|^{2})\mathbf{r}_{n}(\hat{\tau} + 1:\hat{\tau} + N, 1)$$
[Eqn 30]

$$\tilde{\mathbf{d}}_{n+1} = (|\hat{h}_1|^2 + |\hat{h}_2|^2)\mathbf{r}_{n+1}(1:N,1)$$
 [Eqn 31]

# V. SYMBOL ERROR RATE

The symbol error rate (SER) of orthogonal STBC over Rayleigh block flat-fading channels can be evaluated using the well-known approach of averaging the conditional SE R,  $P(E | \gamma)$ , over the probability density function,  $p_{\gamma}(\gamma)$ , of the instantaneous signal-to-noise ratio (SNR) per symbol,  $\gamma$ , as shown below

$$\mathbf{SER} = \begin{bmatrix} \tilde{\mathbf{p}}(\mathbf{E} | \gamma) \mathbf{p}_{\gamma}(\gamma) \mathbf{d} \gamma \qquad [Eqn 32] \end{bmatrix}$$

The analysis done by Shin and Hong Lee<sup>9</sup> yields the closed form SER of STBC for *M*-PSK signals transmitted over a Rayleigh block flat-fading channels as

$$\mathbf{SER} = \boldsymbol{\varphi}_{\gamma}(g_{MPSK}) \left[ \frac{1}{2\sqrt{\pi}} \frac{\Gamma\left[n_{T}n_{R} + \frac{1}{2}\right]}{\Gamma(n_{T}n_{R} + 1)} \cdot A + \frac{\sqrt{I - g_{MPSK}}}{\pi} \cdot B \right] \qquad [\text{Eqn 33}]$$

where

$$A = {}_{2}F_{1}\left[n_{7}n_{R}, \frac{1}{2}; n_{7}n_{R}+1; \frac{1}{1+g_{MPSK} \bar{\gamma}}\right]$$
 [Eqn 34]

![](_page_3_Figure_38.jpeg)

FIGURE 8 Illustration of  $r_a$  and  $r_b$  for  $\tau < 0$ 

S Afr J Sci

$$B = \mathbf{F}_{1} \left[ \frac{1}{2}; n_{T} n_{R}, \frac{1}{2} - n_{T} n_{R}; \frac{3}{2}; \frac{1 - \mathcal{G}_{MPSK}}{1 - \mathcal{G}_{MPSK} \bar{\gamma}}, 1 - \mathcal{G}_{MPSK} \right]$$
[Eqn 35]

$$g_{MPSK} = \sin^2(\pi/M), \,\overline{\gamma} = (E_s/n_T R N_0)$$
 [Eqn 36]

with  $E_s$  being the symbol energy and R being the transmission rate, the numbers  $n_r$  and  $n_R$  are the numbers of transmit and receive antennas, respectively,  $\Gamma(.)$  represents the gamma function,  ${}_2\mathbf{F}_1$  and  $\mathbf{F}_1$  represent the Gauss and Appell hypergeometric functions respectively and  $\varphi$  is the moment generating function for the instantaneous SNR given by

$$\varphi(g_{MPSK}) = (1 + g_{MPSK}\overline{\gamma})^{-n_{1}n_{R}}$$
[Eqn 37]

# VI. SIMULATION RESULTS

In our simulations, each block contains 140 symbols of which 112 are used for data and L = 14 for the pilot sequence. When choosing the pilot sequence length, there is a trade-off between estimation performance and bandwidth efficiency. With this in mind, a sequence length of 14 was chosen as a reasonable balance between the two. The 4-PSK modulation was used, and the channel and noise parameters used were as described from [Eqn 3]. The channels were assumed to be unknown and hence needed to be estimated. Unless otherwise stated, the delay was assumed to remain constant over each frame, but was allowed to vary randomly from frame to frame. The delays were uniformly distributed between -(L-1) and (L-1). The SNR values that were used refer to the ratio between symbol and noise energy. The single-input-single-output (SISO) equaliser used was a minimum mean square error (MMSE) equaliser.

### **Channel estimation performance**

Channel and delay estimation was normally implemented using a training sequence or pilot sequence. Tourki and Deneire<sup>7</sup> did not discuss the method to design the pilot sequence. To estimate channel and delay, it is not merely enough to simply transmit a known set of symbols as pilot sequences. These sequences have to be carefully designed in order to achieve the best channel estimation performance possible. The design of the pilot sequence in frequency flat-fading channels for asynchronous cooperative communication systems has been discussed by Padayachee<sup>10,11</sup>. To derive optimal pilot sequences, the base station has to have information about the channel delay. In Padayachee<sup>10,11</sup>, a packet transmit scheme was proposed to enable the base stations to use an estimate of the delay to select the corresponding optimal pilot sequences for that specific delay.

The scheme can be divided into three phases. In the first phase, the base stations transmit x pilot frames consisting of pilot

With the second second

FIGURE 9 Minimum square error (MSE) of the channel estimation: normal scheme vs. packet scheme

symbols only. The mobile receiver then uses these frames to obtain an average estimate of the channel delay, and then transmits the estimated delay back to the base stations via the feedback channel in phase two. In phase three, the base stations use this delay estimate to select the corresponding optimal pilot sequences for channel estimation, to be used in the next *y* normal frames consisting of data and pilot symbols. It is assumed that the delay remains constant over each round of the above three phases, but is allowed to vary from round to round.

In our simulations, we also use the two transmit schemes. Figure 9 shows the MSE performance of the channel estimation. It has the following plots:

- MSE of the channel estimation when the channel and delay are unknown.
- MSE of the channel estimation when the channel and delay are unknown and where the packet scheme is used. After every 200 data frames, five pilot symbol frames are sent at an SNR of 10 dB.
- CRB for channel estimation.

The CRB serves as a fundamental lower bound on the performance of any unbiased estimator. The CRB for channel estimation as derived by Berriche et al.<sup>12</sup> is given by

$\mathbf{CRB}(h) = tr\{N_0[\mathbf{S} < \boldsymbol{\tau} >]^{\mathrm{H}} \mathbf{S} < \boldsymbol{\tau} >]^{-1}\}$	[Eqn 38]
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where *tr*(.) represents the trace operator. It is important to note, however, that this bound was derived assuming that the delay was a known parameter, therefore it is only used here in order to obtain a tractable comparison.

It can be observed from Figure 9 that, for low SNRs, the channel estimation of the normal scheme significantly differs from the CRB, due to the relatively high error rate of the delay estimation. However, using the packet scheme, which has a relatively low error rate, the channel estimation performance practically achieves the CRB. This is because feedback is used in the packet transmit scheme to choose an optimal pilot sequence.

## SER performance

The SER derivation [Eqn 33] was done assuming that the channel and delay were known parameters, as obtaining a closed form expression of the SER would otherwise prove rather complex. This assumption was made in order to obtain a tractable comparison, and its result is plotted in Figure 10 as the 'ideal'.

From Figure 10, it can be observed that at low SNRs, the normal scheme performance is between 1 dB and 2 dB worse than the 'ideal', whereas the packet scheme is approximately 0.5 dB off the 'ideal'. This performance demonstrates that if the

![](_page_4_Figure_25.jpeg)

FIGURE 10 Symbol error rate (SER) of the channel estimation: normal scheme vs. packet scheme

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packet scheme is used, relaxing the known channel and delay assumption only results in a mere 0.5 dB difference. Also, if the channel is assumed to be known, the delay estimation exhibits very low error rate and the SER performance achieves the 'ideal', demonstrating that the channel estimation dominates the system performance.

# VII. CONCLUSION

In this paper, the scheme proposed by Tourki and Deneire<sup>7</sup> was extended to accommodate negative delays in base-station-based cooperative communication systems. The various concepts and modifications were explained in detail. A block form of the decoding scheme was also presented, which allowed for a simple modification to accommodate negative delays. Both the normal scheme and the packet scheme were simulated. It was shown via the simulations that the packet scheme outperformed the normal scheme by achieving the CRB for channel estimation. As far as the SER is concerned, the packet scheme demonstrated that performance gains were achievable at minimal expense in bandwidth efficiency. The only limitation for the packet scheme is that the delay remains constant over the three phases. Possible future work would be to extend the scheme presented in this paper into frequency-selective fading channels.

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